

# GCSE MATHEMATICS 8300/1H

Higher Tier Paper 1 Non-Calculator

Mark scheme

June 2024

Version: 1.0 Final



Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

No student should be disadvantaged on the basis of their gender identity and/or how they refer to the gender identity of others in their exam responses.

A consistent use of 'they/them' as a singular and pronouns beyond 'she/her' or 'he/him' will be credited in exam responses in line with existing mark scheme criteria.

Further copies of this mark scheme are available from aga.org.uk

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# **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

M	Method marks are awarded for a correct method which could lead to a correct answer.
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
M dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles.

## **Diagrams**

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

#### Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

#### Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

## Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

## Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

#### **Further work**

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

#### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

#### Work not replaced

Erased or crossed out work that is still legible should be marked.

## Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

## Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

#### Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

Q	Answer	Mark	Comments	
	$(12^2 =) 144$ or $(\sqrt{36} =) 6 \text{ or } (\frac{1}{3} \times \sqrt{36} =) 2$	M1	implied by correct answer accept $(\sqrt{36} =) \pm 6$ or $(\frac{1}{3})$	× √36 =) ±2
and $ (\frac{1}{3} \times \sqrt{36} =) 2 $ M1dep $ or \frac{432}{6}  oe  fraction $			implied by correct answer $144 \times \frac{1}{2}$ or $\frac{432}{6}$ oe fraction implies If accept $(\frac{1}{3} \times \sqrt{36} =) \pm 2$	M1M1
1	72	A1	accept ±72 SC2 288	
		ditional G	iuldance	
	–72 only			M1M1A0
	Condone missing brackets if recovered eg $12^2 \div \frac{1}{3} \times 6$ with answer 72	ed		M1M1A1
	$\frac{144}{\frac{1}{3} \times 6}$ with no further correct work			M1M0A0
	Using a decimal for $\frac{1}{3}$ must be recov	ered		

Q	Answer	Mark	Comments
2	[31, 34]	B1	

Q	Answer	Mark	Comments	
	$\begin{pmatrix} 3 \\ -7 \end{pmatrix}$	B1		
3	Additional Guidance			
	Condone + sign and/or fraction line	B1		
	(3, -7)		В0	

Q	Answer	Mark	Comments
4(a)	8350	B1	

Q	Answer	Mark	Comments
4(b)	8449	B1	

Q	Answer	Mark	Comments
5(a)	Fully correct diagram   G  21  7  15  35	В3	B2 two or three correct numbers in correct positions B1 one correct number in correct position
	Ado	ditional G	Guidance
	Only mark the numbers in the diagram	m	

Q	Answer	Mark	Comments	
	$\frac{7}{22}$ or 0.318() or 31.8()%	B1ft	oe fraction, decimal or percentage correct or ft their diagram	
	Ade	ditional G	Guidance	
	Answer as a ratio with or without $\frac{7}{22}$ seen			
5(b)	Answer in words with $\frac{7}{22}$ seen			
	Answer in words without $\frac{7}{22}$ seen $\frac{7}{22}$ seen with incorrect conversion to decimal or percentage			
	Ignore any attempt to simplify or conv	ert their -	7 22	B1ft

Q	Answer	Mark	Comments	
	At least 3 points correctly plotted	M1	$\pm \frac{1}{2}$ square	
	All 4 points correctly plotted and joined with straight lines	A1	$\pm \frac{1}{2}$ square lines may be dashed	
6a	Additional Guidance			
	Mark intention for straight lines			
	Condone one continuous, smooth cu	rve		
	Ignore the graph before 2015 and after 2022			
	Ignore a line of best fit			

Q	Answer	Mark	Comments	
	[82, 90]	B1		
6b	Ad	ditional G	Guidance	
	Answer in range with or without work	ing, with r	o graph or incorrect graph	B1

Q	Answer	Mark	Comments	
	Correct statement	B1	ead of the	
	Ad	ditional C	Guidance	
	Check diagram			
	For 'vertical' accept anything that imp	olies she h	nas used the wrong height	
	Condone 'length' to mean 'height' or	ʻslant heiç	ghť	
	12 or 13 circled on the diagram must be accompanied by a supporting statement			
7a	Indicates '12' in the calculation			
	She should have done $\pi \times 5 \times 13$			
	It should be 65π			
	She used the wrong height / the (value	ue of) $l$ is	wrong	B1
	She hasn't used the slant height (she	used the	(vertical) height)	B1
	She hasn't used the 13			B1
	She hasn't used the 13 and should be 5 $\times$ 12 $\times$ 13 $\times$ $\pi$			В0
	The multiplication used the wrong number(s)			В0
	She hasn't used a value for $\pi$			В0
	An incorrect statement with a correct statement			
	eg she used 13 instead of 12 and did	dn't squar	e the radius	B0

Q	Answer	Mark	Comments	
7b	$\pi \times 5 \times 5$ or $25\pi$ or $3 \times 5 \times 5$	M1	oe accept [3.14, 3.142] or $\frac{22}{7}$	for π
15	75	A1		
	Ad	ditional G	Guidance	
	π25			M1

Q	Answer	Mark	Comments	
	'More than' indicated or implied by statement and valid reason  B1 eg valid reasons 3.14 is greater (than 3) Beth's number is bigger (that (the correct answer is) 78.5 answer to (b) less than 78.5			(with their
	Ade	ditional G	Guidance	
	If calculations are used, the outcome	s must be	correct	
	Accept 78 or 79 for 78.5 unless from	incorrect	working	
	'Less than' indicated  Do not penalise use of the same incorrect formula in (b) and (c)  eg 3 × 10 = 30 in (b) and 3.14 × 10 = 31.4 in (c) with 'More than' ticked  B1  Ignore a non-contradictory reason with a correct reason  eg 3.14 is bigger than 3 and nearer the true value of pi  Acceptable reasons			
7c				
	Adam has rounded (pi) down / Adam	only used	d 3	B1
	There is an extra 0.14 to multiply by			B1
	Her number has decimal places  Her number is to more significant figures			
	Non-acceptable reasons			
	3.14 will give a bigger answer / 3.14 i	s more a	ccurate	В0

Q	Answer	Mark	Comments	
	7x - 4x or $3xor 4x - 7x or -3xor -22 - 29 or -51or 22 + 29 or 51$	M1		
	3x = 51 or $-3x = -51$	A1	$\frac{51}{3}$ or $\frac{-51}{-3}$ implies M1A1 implied by correct answer	
8	17	A1ft	ft M1A0 from an equation of $\pm 3x = a$ or $bx = \pm 51$	the form
	Ad	ditional G	Guidance	
	Trial and improvement scores 0 or 3			
	If a follow through answer does not s fraction, mixed number or decimal to		•	
	eg from $3x = 7$ accept $\frac{7}{3}$ or $2\frac{1}{3}$ or 2.3 or better			M1A0A1ft
	Ignore any attempt to convert a correct ft fraction			
	Embedded answer			M1A1A0

Q	Answer	Mark	Comments
	26(.0) 16.4	M1	oe eg $\frac{13}{8.2}$ or $1\frac{9.6}{16.4}$
	$\frac{260}{164}$ or $1\frac{96}{164}$	A1	oe with no decimals eg $\frac{130}{82}$ or $\frac{2600}{1640}$ implied by correct answer
9	$\frac{65}{41}$ or $1\frac{24}{41}$	B1ft	ft correct simplification of their fraction using the digits 26 and 164  SC2 $\frac{41}{65}$ SC1 $\frac{65}{106}$ (total area as denominator)
	Ad	ditional G	auidance
	Ignore units		
	Ignore an incorrect conversion of $\frac{65}{41}$	to a mix	ed number M1A1B1
	$\frac{26(.0)}{16.4} = \frac{2600}{164} = \frac{650}{41}$		M1A0B1ft

Q	Answer	Mark	Comments	
	Line joining open circles above, on or below –2 and 4	B1	condone arrows on a correct open circles	t line with
	Additional Guidance			
10a	Mark intention			
	If the student has drawn the circles on the line, they must have drawn their own line connecting the circles			
	Closed circle(s)			В0

Q	Answer	Mark	Comments	
	$5y \ge 11 - 14 \text{ or } 5y \ge -3$ or $14 - 11 \ge -5y \text{ or } 3 \ge -5y$ or $y + \frac{14}{5} \ge \frac{11}{5}$ or $-\frac{3}{5}$	M1	oe fractions or decimals  may be seen in an equation	or inequality
10b	$y \geqslant -\frac{3}{5} \text{ or } -\frac{3}{5} \leqslant y$	A1	oe fraction or decimal for $-\frac{3}{5}$	
	Ad	ditional G	Guidance	
	Allow use of other inequality signs or	= if recov	ered	
	Accept any letter for y			
	Condone $\frac{-3}{5}$ or $\frac{3}{-5}$ for $-\frac{3}{5}$			
	Ignore any attempt to convert $-\frac{3}{5}$ to a	a decimal		
	$y \geqslant -\frac{3}{5}$ in working and $-\frac{3}{5}$ on answ	er line		M1A0

Q	Answer	Mark	Comments	
	Enlarge(ment)	B1		
	$\frac{1}{2}$	B1	oe condone half	
	(1, -7)	B1	condone missing bracket(s)	
11	Additional Guidance			
	For the third mark, a vector on its ow	n does no	t imply a translation	
	Do not accept halved or half the size			
	Multiple transformations stated or implied			B0B0B0

Q	Answer	Mark	Comments	
	$2 \times 12 \times \pi$ or $24\pi$ or $\frac{60}{360}$ or division by 6	M1	oe accept [3.14, 3.142] or $\frac{22}{7}$ accept use of 0.17 or better	
12	$\frac{60}{360} \times 2 \times 12 \times \pi$	M1dep	oe eg $\frac{24\pi}{6}$	6
	4π	A1	condone π4	
	Ad	ditional G	Guidance	
	Answer $24\pi$ from $\pi \times 12^2 \times \frac{60}{360}$ scores M1 for $\frac{60}{360}$ M1M0A			M1M0A0

Q	Answer	Mark	Comments	
	<ul> <li>Fully correct diagram with all these 6 conditions met</li> <li>Line length 6 cm from B</li> <li>Line perpendicular to AB from B</li> <li>Line length 7 cm parallel to AB</li> <li>Area of pentagon = 54 cm<sup>2</sup></li> <li>Pentagon has exactly one line of symmetry</li> <li>Labelled pentagon</li> </ul>	B4	B3 5 conditions met B2 4 conditions met B1 3 conditions met  condone label <i>E</i> missing	
13		ditional G	Guidance	
	Mark intention	lines of a	v rac no a tru r	
	Ignore any lines inside the shape eg		<u> </u>	
	A diagram that is not a pentagon can	only mee	t the first 3 conditions	B0 or B1
				B4

Q	Answer	Mark	Comments
	Alternative method 1: elimination		
	at least one correct equation	M1	eg $4x + 3y = 4.7(0)$ or $5x + y = 4.5(0)$ or $15x + 3y = 13.5(0)$ or $9x + 4y = 9.2(0)$ may work in pounds or pence any letters
14	correctly multiplies one or two correct equations to equate coefficients of $x$ or $y$	M1dep	eg 4x + 3y = 4.7(0) and 15x + 3y = 13.5(0) or 20x + 15y = 23.5(0) and 20x + 4y = 18.(00)
	correctly adds or subtracts correct equations to eliminate one variable	M1dep	eg 11x = 8.8(0) or 11y = 5.5(0) may be implied by one correct value of $x$ or $y$ with M2 scored
	chocolate bar £0.80 and packet of mints £0.50 or chocolate bar 80p and packet of mints 50p	A1	correct money notation condone £0.80p and £0.50p

# Question 14 continues on the next page

	Alternative method 2: substitution			
	4x + 3y = 4.7(0) or $5x + y = 4.5(0)$ or $15x + 3y = 13.5(0)$ or $9x + 4y = 9.2(0)$	M1	oe may work in pounds or pence any letters	
	correctly makes x or y the subject of a correct equation	M1dep	eg $x = \frac{4.7(0) - 3y}{4} \text{ or } x = \frac{4.5(0) - y}{5}$ or $y = \frac{4.7(0) - 4x}{3} \text{ or } y = 4.5(0) - 5x$	
14 cont	correctly substitutes to eliminate a variable	M1dep	eg $5\frac{(4.7(0)-3y)}{4} + y = 4.5(0)$ or $4\frac{(4.5(0)-y)}{5} + 3y = 4.7(0)$ or $5x + \frac{4.7(0)-4x}{3} = 4.5(0)$ or $4x + 3(4.5(0) - 5x) = 4.7(0)$ may be implied by one correct value or $y$ with M2 scored	of x
	chocolate bar £0.80 and packet of mints £0.50 or chocolate bar 80p and packet of mints 50p	A1	correct money notation condone £0.80p and £0.50p	
	Ad	ditional G	uidance	
	Up to M3 may be awarded for correct work with no answer or incorrect answer if this is seen amongst multiple attempts			
	Condone multiple letters in equations	eg cb fo	r x	
	Trial and improvement is 0, 3 (incorre	ect money	notation) or 4 (fully correct)	
	Final answer chocolate bar £0.8 and	packet o	f mints £0.5 M3A	<b>A</b> 0
	Final answer chocolate bar 0.80p an	d packet	of mints 0.50p M3A	40

Q	Answer	Mark	Comments	
	14 and 15	B1	either order	
15(0)	Additional Guidance			
15(a)	Ignore incorrect calculations			
	Answer 14 <sup>2</sup> and 15 <sup>2</sup>			В0

Q	Answer	Mark	Comments
15(b)	$2^{7}$ or 128 or $7^{3}$ or 343 or $(5 \times) \sqrt[3]{1000000}$ or $(5 \times) 100$ or 500	M1	
	At least two of 128, 343 and 500 or 471	A1	
	471 and 500	A1	

Q	Answer	Mark	Comments	
	A correct comparison of the average age of the two clubs	B1	eg the average (age) of the cyclists was higher/older the median (age) of the swimming club	
			was lower/younger, (so the a lower/younger)	
	A correct comparison of the consistency of the ages of the two		eg the cycling club has mor ages	e consistent
	clubs	B1	the interquartile range of the club was higher, so they wer consistent in age	•
	Ad	ditional C	Guidance	
	Statements must be comparisons			
	eg1 (the average age at) the cycling club was higher			B1
16	eg2 (the average age at) the cycling club was high			B0
	Statements reversed	В0		
	Do not allow incorrect values support			
	Ignore non-contradictory statements			
	Average age statements			
	The swimming club are (8.5 years) younger (on average)			B1
	Cycling club members are (8.5 years) older (on average)			B1
	Younger people prefer swimming (to cycling)			B1
	Young people prefer swimming (to cycling)			В0
	Average age has 8.5 years difference			В0
	The cycling club has more older people			В0

Additional guidance for this question continues on the next page

Q	Additional Guidance cont					
	Consistency statements					
	The cycling club is more consistent / has better consistency					
	There is a smaller (interquartile) range for cycling, so it's more consistent	B1				
	Ages of the cycling club are closer together	B1				
	Consistency at the cycling club is bigger					
	Consistency at the cycling club is smaller	В0				
	More people are in the same age group in the cycling club	В0				
	The difference in interquartile range is 2.7	В0				
	The swimming club had a higher (interquartile) range	В0				
	The swimming club had a higher range of ages	В0				
	More of an age gap / age range in the swimming club than the cycling club	В0				

Q	Answer	Mark	Comments	
	Alternative method 1: multiplies by $x$ first			
	xy = 3x + 7	M1	allow yx for xy throughout	
	xy - 3x = 7	M1dep	oe collection of terms	
	or $3x - xy = -7$	Wirdep		
	x(y-3)=7			
	or $y = y$	M1dep		
	$\frac{7}{y-3}$ or $\frac{-7}{3-y}$			
	7 or7		oe in the form $x =$	
	$x = \frac{7}{y-3}$ or $x = \frac{-7}{3-y}$	A1	may have brackets on the denominator	
17	Alternative method 2: splits up the fraction first			
	$y = 3 + \frac{7}{x}$ or $y - \frac{7}{x} = 3$	M1	allow $\frac{3x}{x}$ for 3	
	$y-3 = \frac{7}{x}$ or $3-y = -\frac{7}{x}$	M1dep		
	$\frac{1}{y-3} = \frac{x}{7}$			
	or $x(y-3) = 7$ or $x(3-y) = -7$ or	M1dep		
	$\frac{7}{y-3}$ or $\frac{-7}{3-y}$			
	$x = \frac{7}{y-3}$ or $x = \frac{-7}{3-y}$	A1	oe in the form $x =$ may have brackets on the denominator	

# Additional guidance for this question is on the next page

	Additional Guidance		
	Up to M2 may be awarded for correct work with no answer or incorrect answer if this is seen amongst multiple attempts		
17	$\frac{7}{y-3}$ on answer line with $x = \frac{7}{y-3}$ in working		
cont	Allow the equation with x on the right, eg $\frac{7}{y-3} = x$	M3A1	
	Condone $x = 7/y - 3$ if not from incorrect working	M3A1	
	Allow appropriate × or ÷ signs throughout for up to M3		

Q	Answer	Mark	Comments		
	$x^2 + y^2 = 6^2$ or $x^2 + y^2 = 36$	B1	oe equation		
40	Additional Guidance				
18	$x^2 + y^2 = 6^2$ followed by an incorrect evaluation of $6^2$				
	Condone $x^2 + y^2 = r^2$ and $r = 6$			B1	

Q	Answer	Mark	Comments	
	Alternative method 1: expressing $C$ in terms of $A$			
	$(C =) \frac{5}{2}A$	M1	oe eg $(C =) A + 1.5A$ or $(C =) 2.5A$	
	$\left(\frac{C}{B} = \right) \frac{\frac{5}{2}A}{\frac{7}{4}A}$	M1dep	oe fraction with $A$ on numerator and denominator $ \text{eg } \left(\frac{C}{B} = \right) \frac{2.5A}{1.75A} \text{ or } \frac{5}{2}A \div \frac{7}{4}A $	
	$\left(\frac{C}{B} = \right) \frac{\frac{5}{2}}{\frac{7}{4}}$ or $14C = 20B$	M1dep	oe fraction with $A$ eliminated $ \text{eg } \left( \frac{C}{B} \right) = \frac{2.5}{1.75} $ oe method to eliminate $A$	
19	$\frac{10}{7}$ or $1\frac{3}{7}$	A1	oe fraction $SC3 \ \frac{7}{10} \text{ oe fraction with } A \text{ eliminated}$ $SC2 \ \frac{6}{7} \text{ oe fraction with } A \text{ eliminated}$	
	Alternative method 2: using a value for A			
	Chooses a value for $A$ works out the correct value of $B$ or $C$	M1	eg $A = 100$ and $B = 175$ or $A = 20$ and $C = 50$	
	Chooses a value for $A$ and works out correct values for $B$ and $C$	M1dep	eg $A = 10$ and $B = 17.5$ and $C = 25$	
	Puts the correct values for <i>B</i> and <i>C</i> into fraction form (may have noninteger values)	M1dep	oe eg $\frac{25}{17.5}$	
	$\frac{10}{7}$ or $1\frac{3}{7}$		oe fraction eg $\frac{250}{175}$	
		A1	SC3 $\frac{7}{10}$ oe fraction with $A$ eliminated	
			SC2 $\frac{6}{7}$ oe fraction with $A$ eliminated	

# Additional guidance for this question is on the next page

	Additional Guidance			
	Ignore an incorrect conversion of $\frac{10}{7}$ to a mixed number			
19 cont	$\frac{6}{7}$ is from taking $C$ as 1.5 $A$	SC2		
Cont	Condone the inclusion of <i>B</i> in the fraction eg $(C = )\frac{10}{7}(\times) B$ or $(C = )\frac{10B}{7}(\times) B$	M3A1		
	Alt 2 The chosen value of $A$ does not need to be explicitly stated if method is shown and working is unambiguous or values are in correct proportion			

Q	Answer	Mark	Comments	
	a = -3	B1		
20	8 or $(\text{their} -3)^2 - 1$ correctly evaluated 4	B1ft B1ft		
	or their 8 ÷ 2 correctly evaluated	DIII		
	Additional Guidance			
	a = -3 $b = -10$ $c = -5$			B1B0B1ft

Q	Answer	Mark	Comments		
	Alternative method 1: using $x = 1.018$				
	Multiplication by power of 10	M1	eg $10x = 10.18$ or $100x = 101.81$ or $1000x = 1018.18$ any or no letter		
	Correct equation formed from subtraction of two equations to eliminate recurring digits	M1dep	eg $99x = 100.8$ or $990x = 1008$ or $x = \frac{1008}{990}$		
	$(x =)$ $\frac{1008}{990}$ and $\frac{56}{55}$ with no incorrect working	A1	oe from using different powers of 10		
	Alternative method 2: using $x = 0.018$				
21	Multiplication by power of 10	M1	eg $10x = 0.1818$ or $100x = 1.818$ or $1000x = 18.18$ any or no letter		
	Correct equation formed from subtraction of two equations to eliminate recurring digits	M1dep	eg $99x = 1.8$ or $990x = 18$ or $x = \frac{1.8}{99}$		
	$(x =) \ \frac{1.8}{99} \ \text{or} \ \frac{18}{990}$ and $(x =) \ \frac{1}{55} \ \text{and} \ \frac{56}{55}$ or $\frac{100.8}{99} \ \text{or} \ \frac{1008}{990} \ \text{and} \ \frac{56}{55}$ with no incorrect working	A1	oe from using different powers of 10		

# Question 21 continues on the next page

Q	Answer	Mark	Comments		
	Alternative method 3: using $x = 1.018$ and addition				
	Multiplication by power of 10	M1	eg $10x = 10.18$ or $100x = 101.81$ or $1000x = 1018.18$ any or no letter		
	Correct addition of two correct equations leading to 0.9 recurring	M1dep	eg $110x = 111.99$ or $1100x = 1119.99$		
21 cont	$(x =)$ $\frac{112}{110}$ and $\frac{56}{55}$ with no incorrect working	A1	oe from using different powe	ers of 10	
Cont	Additional Guidance				
	Up to M2 may be awarded for correct work with no answer or incorrect answer if this is seen amongst multiple attempts				
	For all marks, numbers must be correct				
	Working with 1.018018018 scores				
	Recurring decimals should be denoted by correct notation or at least two of the recurring digits followed by at least two dots				
	In alt1 and alt2 condone incorrect red subtraction is a correct equation	curring not	ation if the result of the		

Q	Answer	Mark	Comments	
	Alternative method 1: drawing AO	and BO a	and sum of angles in a quadrilateral	
	<i>PBO</i> = 90 or	M1	may be seen on diagram or implied by subsequent working	
	<i>PAO</i> = 90		accept rectangle drawn at angle	
	360 - 90 - 90 - 24		oe eg 180 – 24 or 90 – 12	
	or	M1dep		
	156		may be seen on diagram	
	78	A1		
	Alternative method 2: drawing AO	and <i>BO</i> a	and using circle theorems	
	AOB = 2x	M1	may be seen on diagram	
	2x = 156	M1dep		
	78	A1		
	Alternative method 3: drawing AB, sum of angles in a triangle and alt segment			
22	2 <i>PAB</i> + 24 = 180			
	or	M1		
	2 <i>PBA</i> + 24 = 180			
	(180 − 24) ÷ 2 or 78		may be seen on diagram	
	or	M1dep		
	(180 − 24) ÷ 2 or 78			
	<i>x</i> = 78	A1		
	Alternative method 4: drawing PO and AO or BO and sum of angles in a triangle			
	<i>PBO</i> = 90		may be seen on diagram or implied by	
	or	M1	subsequent working	
	<i>PAO</i> = 90		accept rectangle drawn at angle	
	180 – 90 – 12		oe eg 90 – 12	
	or	M1dep		
	78		may be seen on diagram	
	78	A1		

Additional guidance for this question is on the next page

Q	Answer	Mark	Comments		
	Additional Guidance				
22 cont	Answer 78			M1M1A1	
John	Working takes precedence over diag	ram			

Q	Answer	Mark	Comments	
	$\frac{25}{16}$ or $1\frac{9}{16}$	B1	oe with no surds or indices	
	Additional Guidance			
23(a)	Ignore an incorrect conversion of $\frac{25}{16}$ to a mixed number			
	$\frac{5\sqrt{5}\sqrt{5}}{16}$ or $\frac{5^2}{16}$			В0

Q	Answer	Mark	Comments	
23(b)	$4 + 2\sqrt{3} + 2\sqrt{3} + (\sqrt{3})^{2}$ or $4 + 4\sqrt{3} + (\sqrt{3})^{2}$ or $7 + 4\sqrt{3}$	M1	oe 4 terms with at least 3 correct or 3 terms with 2 correct including $4\sqrt{3}$ terms may be seen in a grid	
	$7 \times 2 + 7\sqrt{3} + 2 \times 4\sqrt{3} + 4\sqrt{3} \times \sqrt{3}$ or $8 + 8\sqrt{3} + 6 + 4\sqrt{3} + 4 \times 3 + 3\sqrt{3}$ or $14 + 7\sqrt{3} + 8\sqrt{3} + 12$ or $8 + 4\sqrt{3} + 4\sqrt{3} + 6 + 4\sqrt{3} + 6 + 6$ $+ 3\sqrt{3}$	M1dep	oe full expansion with correct multiplication of their 2, 3 or 4 terms by $(2 + \sqrt{3})$ terms may be seen in a grid	
	$8 + 4\sqrt{3} + 4\sqrt{3} + 6 + 4\sqrt{3} + 6 + 6$ $+ 3\sqrt{3}$ and $26 + 15\sqrt{3}$ or $14 + 7\sqrt{3} + 8\sqrt{3} + 12$ and $26 + 15\sqrt{3}$	A1	oe with full expansion terms may be seen in a grid condone $15\sqrt{3} + 26$	
	Additional Guidance			
	Remember that the answer is given in the question			
	3 may be seen as $(\sqrt{3})^2$ for M1 only			
	Condone missing brackets if multiplications are correct			

Q	Answer	Mark	Comments	3
24(a)	$2k^2 + 3 - (9k + 7) (= 1)$ or $2k^2 - 9k - 4 (= 1)$	M1	oe eg $9k + 7 + 1 = 2k^2 + 3$ or $9k + 8 = 2k^2 + 3$	
	$2k^2 - 9k - 5 (= 0)$	A1	terms in any order implied by $k = 5$ (and $-\frac{1}{2}$ ) or correct answer	
	$(2k+1)(k-5) (= 0)$ or $(k =) \frac{9 \pm \sqrt{9^2 - 4 \times 2 \times -5}}{2 \times 2}$ or $(k =) \frac{9 \pm \sqrt{121}}{4}$ or $(k =) 2.25 \pm \sqrt{7.5625}$	M1	oe correct factorisation or correct use of quadratic formula or correct use of completing the square for their 3-term quadratic	
	$(k =) 5 (or -\frac{1}{2})$	A1ft	ft at least one solution for their 3-term quadratic implied by correct answer	
	54	A1		
	Additional Guidance			
	Answer 54 not from incorrect working			5 marks
	Trial and improvement scores 0 or 5			
	Use of inequalities can score up to M0A0M1A1ftA0			
	Condone 52, 53, 54 on answer line			5 marks
	54 and 4.5			4 marks
	$2k^2 + 3 - 9k + 7 (= 1)$			MO
	$2k^2 - 9k + 9 (= 0)$			A0
	(2k-3)(k-3) (= 0)			M1
	$k = 3 \text{ (or } \frac{3}{2})$			A1ft
	22			A0

Q	Answer	Mark	Comments		
	Alternative method 1				
	$\left(\sqrt{x}+1\right)^2$ or $\left(\sqrt{x}+1\right)\left(\sqrt{x}+1\right)$	M1			
	$\left(\sqrt{x}+1\right)^2$ or $\left(\sqrt{x}+1\right)\left(\sqrt{x}+1\right)$	A1	SC1 takes any square number and shows that $x + 2\sqrt{x} + 1$ gives the next square number		
	and $x + \sqrt{x} + \sqrt{x} + 1$ = $x + 2\sqrt{x} + 1$				
	Alternative method 2				
	$x = n^2$	M1	any letter for n except x		
	$(n+1)^2 = n^2 + 2n + 1$ $= x + 2\sqrt{x} + 1$	A1	SC1 takes any square number and shows that $x + 2\sqrt{x} + 1$ gives the next square number		
24(b)	Alternative method 3				
	$x = n^2$	M1	any letter for n except x		
	$n^{2} + 2\sqrt{n^{2}} + 1 = n^{2} + 2n + 1$ and $(n+1)^{2}$	A1	SC1 takes any square number and shows that $x + 2\sqrt{x} + 1$ gives the next square number		
	Additional Guidance				
	Remember that the answer is given in the question				
	eg for SC1				
	$x = 9, 9 + 2 \times 3 + 1 = 16$			SC1	
	Allow $x^{\frac{1}{2}}$ for $\sqrt{x}$ throughout				
	If only multiplication in a grid is seen then this is not sufficient for A1				

Q	Answer	Mark	Comments	
	Alternative method 1: substitutes values			
	$(\sin 30^\circ =) \frac{1}{2}$		may be seen beside the given expression or in a table	
	or $6 \sin 30^{\circ} = 3$			
	or			
	$(\cos 30^{\circ} =) \frac{\sqrt{3}}{2}$	M1		
	or $2 \cos 30^{\circ} = \sqrt{3}$	IVI I		
	or			
25	$(\tan 30^\circ =) \frac{1}{\sqrt{3}} \text{ or } \frac{\sqrt{3}}{3}$			
	or 4 tan 30° = $\frac{4}{\sqrt{3}}$ or $\frac{4\sqrt{3}}{3}$			
	$6\left(\frac{1}{2}\right)$ and $2\left(\frac{\sqrt{3}}{2}\right)$ and $4\left(\frac{1}{\sqrt{3}}\right)$		oe	
	or			
	$6\left(\frac{1}{2}\right)$ and $2\left(\frac{\sqrt{3}}{2}\right)$ and $4\left(\frac{\sqrt{3}}{3}\right)$	M1dep		
	or			
	$\frac{6}{2}$ and $\frac{2\sqrt{3}}{2}$ and $\frac{4\sqrt{3}}{3}$			
	Processing at least as far as		oe	
	$\frac{6}{2} + \frac{8\sqrt{3}}{2\sqrt{3}}$			
	or $\frac{6}{2} + \frac{8\sqrt{3}\sqrt{3}}{6}$	M1dep		
	or $\frac{6}{2} + \frac{24}{6}$			
	7 from correct working	A1	SC2 4 + $4\sqrt{3}$ oe	

The mark scheme for this question continues on the next page

	Alternative method 2: uses a trig identity			
25 cont	6 sin 30° + 2 cos 30° × 4 $\frac{\sin 30^{\circ}}{\cos 30^{\circ}}$	M1	oe	
	6 sin 30° + 8 sin 30°		oe	
	or	M1dep		
	14 sin 30°			
	$14 \times \frac{1}{2}$	M1dep	oe	
	7 from correct working	A1	SC2 4 + $4\sqrt{3}$ oe	
	Additional Guidance			
	Alt 2 is not on this specification, but may be seen if other qualifications have been studied, eg AQA Certificate – Level 2 Further Maths			
	Incorrect order of operations gives $4 + 4\sqrt{3}$ oe			SC2
	Allow √1 for 1 throughout			