

Please write clearly ir	n block capitals.
Centre number	Candidate number
Surname	
Forename(s)	
Candidate signature	
	I declare this is my own work.

# GCSE MATHEMATICS

H

Higher Tier

Paper 3 Calculator

Monday 13 November 2023 Morning Time allowed: 1 hour 30 minutes

#### **Materials**

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).

#### Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end
  of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

#### Advice

In all calculations, show clearly how you work out your answer.

For Exam	iner's Use
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
26	
TOTAL	

		Answer <b>all</b> q	uestions in the spaces	s provided.	
1	The first four to	13 20	r sequence are  27 r the <i>n</i> th term.		[1 mark]
2		nlarged to squa	$\longrightarrow$	<b>B</b> 8 cm	Not drawn accurately
	Write down the		f the enlargement as a		[1 mark]



Do not write
outside the
hov

Answer cm $\leq$ length $<$ cm $\leq$ At what point does the graph $y=x^3-1$ cross the $y$ axis?	[2 mar
At what point does the graph $y = x^3 - 1$ cross the $y$ axis?	
Answer ( , )	
	[1 ma
Turn over for the next question	

	Salary	Bonus
Last year	£26 000	£4000
This year	6% increase	9% decrease

r it is an increase or a decrease.	[4 m



6 An exhibition	n
-----------------	---

was open for 240 hours

and

had 29760 visitors.

For  $\frac{2}{5}$  of the time the exhibition was open, there were 172 visitors per hour.

For the remaining time, how many visitors per hour were there?

[4	m	a	rk	e'
17		a	ıΝ	3

Answer \_\_\_\_\_

## 7 The first two cube numbers are 1 and 8

Show that

the 3rd cube number can be written as the sum of three different prime numbers.

[3 marks]

11



circle the largest number	3	Circle the largest number
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[1 mark]

5.304

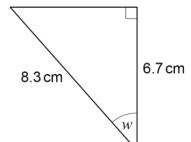
5.344

5.34

5.34

**9** Use trigonometry to work out the size of angle w.

[3 marks]



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w =



10 Two bags contain only green discs and yellow discs.

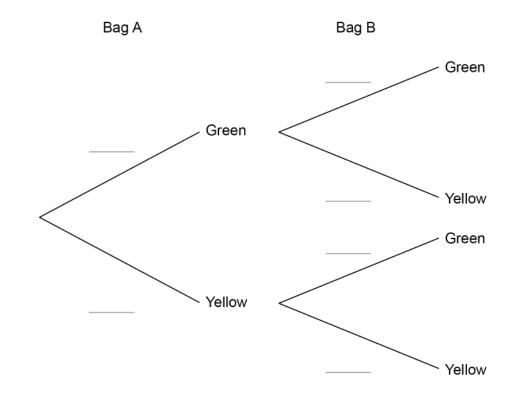
Bag A contains 1 green disc and 4 yellow discs.

Bag B contains 3 green discs and 7 yellow discs.

One disc is picked at random from each bag.

10 (a) Complete the tree diagram with the correct probabilities.

[2 marks]



10 (	(D)	vvork out t	ne probabilit	y tnat <b>both</b>	discs are	green.

Answer

[2	m	а	r	k	s	1

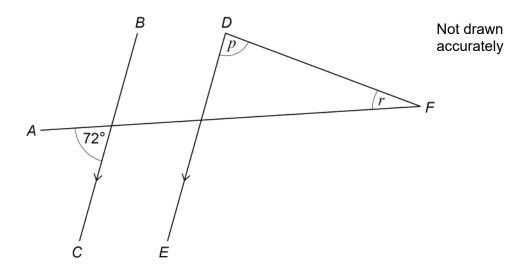
8



11	Solve these simultane	eous equations.	
		7x + 2y = 100	
		3x + 2y = 48	
			[3 marks]
		x = y =	

AF, BC, DE and DF are straight lines.

BC and DE are parallel.



p is three times r.

Work	out	the	size	of	angle	p.
------	-----	-----	------	----	-------	----

6

Turn over ▶

[3 marks]



100 people were asked about the distance they travel from home to work.

The table shows information about the results.

Distance, d (miles)	Frequency
0 ≤ <i>d</i> < 5	21
5 ≤ <i>d</i> < 10	24
10 ≤ <i>d</i> < 20	37
20 ≤ <i>d</i> < 40	18

13	(a)	Write down the g	reatest possible	number of people	who work from home.
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[1 mark]

Answer		
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**13 (b)** One person is chosen at random.

Work out the probability that the person travels at least 10 miles.

[1 mark]

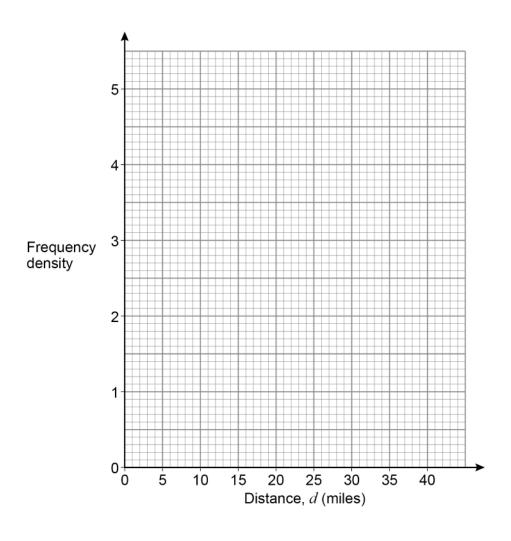
∖nswer			

**13 (c)** The table is repeated.

Distance, d (miles)	Frequency
0 ≤ <i>d</i> < 5	21
5 ≤ <i>d</i> < 10	24
10 ≤ <i>d</i> < 20	37
20 ≤ <i>d</i> < 40	18

Draw a histogram to represent the results.

[3 marks]



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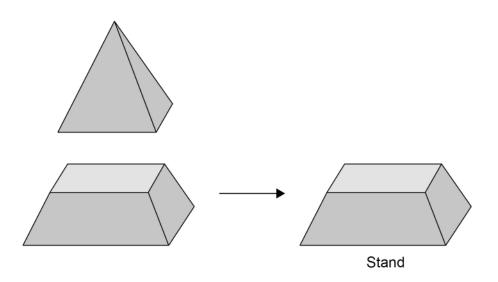
**14** A solid trophy consists of a stand and a player.



Trophy

The stand is made by removing a small pyramid from a large pyramid.

Large pyramid Square base, edge 8 cm Perpendicular height 16 cmSmall pyramid Square base, edge 5 cm Perpendicular height 10 cm



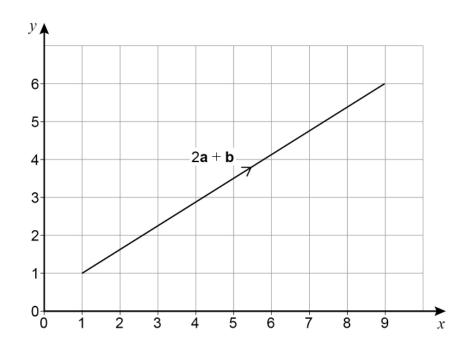
Volume of a pyramid =  $\frac{1}{3}$  × area of base × perpendicular height

14 (a)	Show that the volume of the <b>stand</b> is 258 cm <sup>3</sup>	[2 marks]	Do not write outside the box
14 (b)	The trophy is made from a metal of density 7.5 grams per cm <sup>3</sup> The <b>total</b> mass of the trophy is 2340 grams.  Work out the volume of the <b>player</b> .	[2 marks]	
	Answer	cm <sup>3</sup>	



**15**  $\mathbf{a} = \begin{pmatrix} m \\ 3 \end{pmatrix} \qquad \mathbf{b} = \begin{pmatrix} -4 \\ p \end{pmatrix}$ 

The diagram shows the vector  $2\mathbf{a} + \mathbf{b}$ 



Work out the values of m and p.

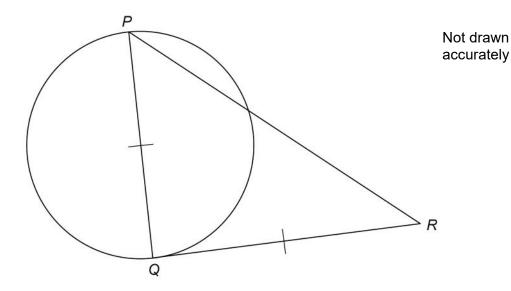
[4 marks]

PQ is a diameter of a circle.

QR is a tangent to the circle.

$$PQ = QR$$

$$PR = 10 \, cm$$



Work out the radius of the circle.

Give your answer as a decimal.

Answer

·	[3 marks]

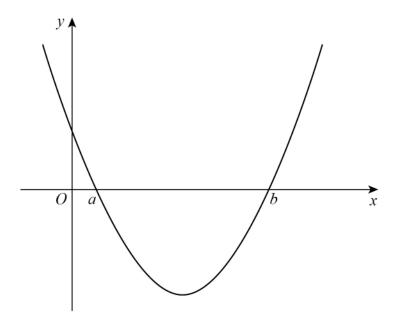
Turn over ►



cm

Here is a sketch of the quadratic graph y = f(x)

The graph crosses the *x*-axis at x = a and x = b



Write an expression for the *x*-coordinate of the turning point.

[1 mark]

Answer			
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Simplify $\frac{2(x+4)^5}{(x+4)^3}$ Give your answer in the form $ax^2 + bx + c$ where $a$ , $b$ and $c$ are integers. [3 marks]				
Give your answer in the form $ax^2 + bx + c$ where $a$ , $b$ and $c$ are integers. [3 marks]	Simplify $\frac{2(x+4)}{(x+4)^3}$	5 3		
	Give your answer in	in the form $ax^2 + bx + a$	c where $a,b$ and $c$ are integer	ers. [3 marks]
	А	nswer		

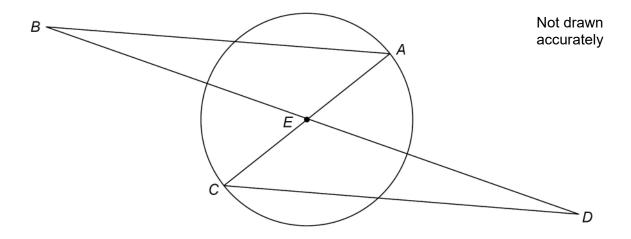
Turn over for the next question

4





19	AC is a diameter of a circle, centre E.
	E is the midpoint of BD.



Prove that triangle ABE is congruent to triangle CDE.	[4 marks]



20	Solve	2x(x+10) = 5x - 18	[4 marks]	Do not v outside box
		Answer		

Turn over for the next question

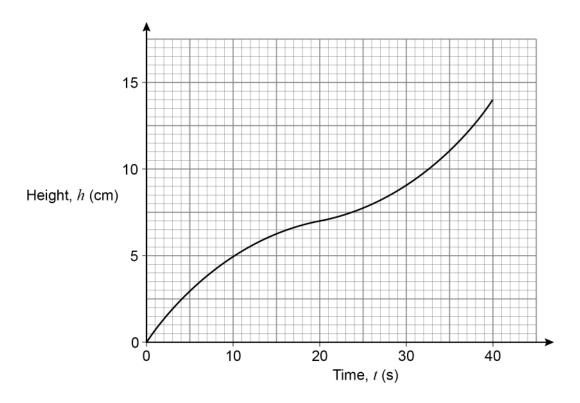




21 Water flows from a tap at a constant rate.

A container is filled with water from the tap in 40 seconds.

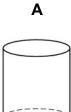
The graph shows the height, h centimetres, of the water after time, t seconds.



**21** (a) The container is one of these shapes.

Circle the letter of the correct shape.

[1 mark]









D

21 (b)	By drawing a tangent on the graph,			
	estimate the rate at which the height is increasing when $t = 10$			
	Answer cm/s			
22	Write $\frac{7}{2a^2} - \frac{3}{5a}$ as a single fraction in its simplest form.			
		[2 marks]		
	Answer			

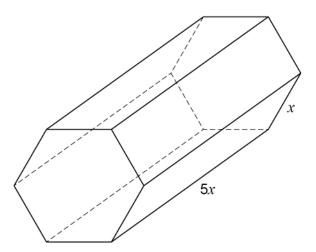
5



A chocolate box in the shape of a prism is being designed.

All lengths are in centimetres.

The cross section is a regular hexagon with side x. The length is 5x



An expression for the area of the cross section, in cm<sup>2</sup>, is  $\frac{3\sqrt{3}}{2}x^2$ 

The **total** surface area of the box must be less than 650 cm<sup>2</sup>

Work out the largest possible **integer** value of x.

Answer

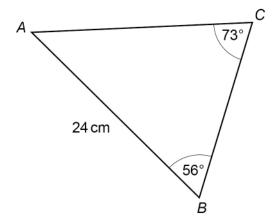
You **must** show your working.

You must snow your working.	[4 marks]

Work out the area of triangle ABC.

Answer

[4 marks]



Not drawn accurately

8

Turn over ▶

 $cm^2$ 



25	a is three quarters of $c$	
	6b = 5c	
	Work out the ratio $a:b:c$	
	Give your answer in its simplest form, where $a$ , $b$ and $c$ are integers.	
		[3 marks]
	Answer : :	



26	In a game, these numbered tiles are in a bag.	Do not write outside the box
	5     5     5       3     3     2	
	To play the game  Choose tiles at random one at a time and do not replace the tiles.  You win if at any stage the total of the numbers on your tiles is 10	
	Amber plays the game once.  Work out the probability that she wins.  [4 m	arks]
	Answer	



**27** (a) The graph of  $y = x^3$  is translated to the graph of  $y = (x-2)^3$ 

Write down the translation vector.

[1 mark]

Answer

**27 (b)** The graph of y = 5x + 4 is reflected in the *y*-axis.

Write down the equation of the reflected graph.

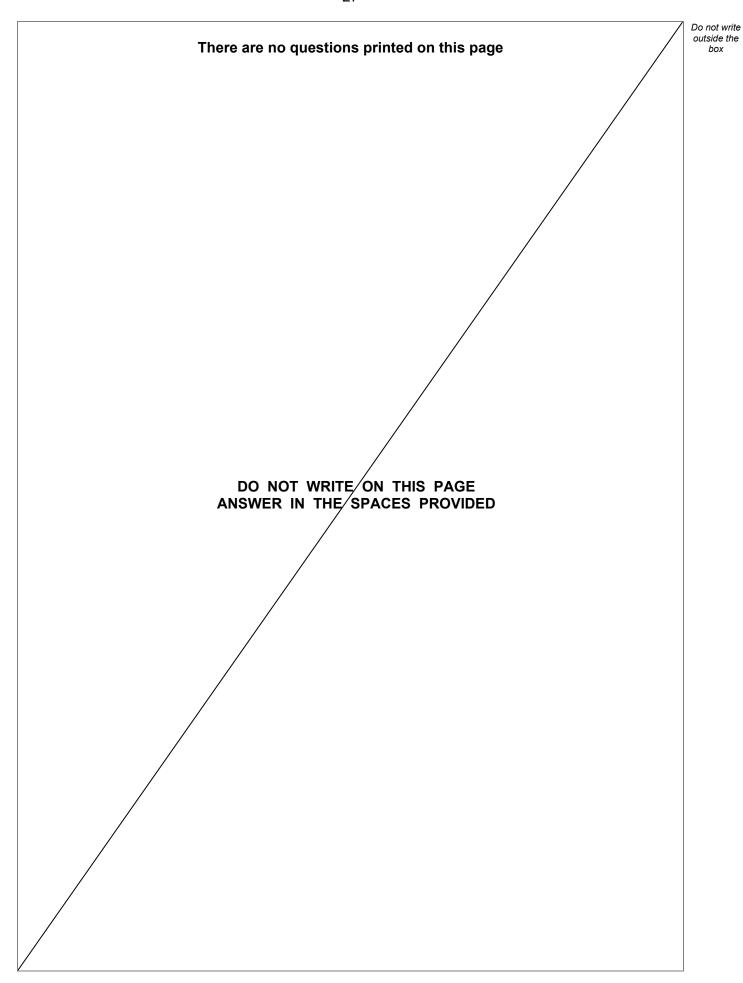
[1 mark]

Answer \_\_\_\_\_

**END OF QUESTIONS** 

2







Question number	Additional page, if required. Write the question numbers in the left-hand margin.



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32 Do not write outside the There are no questions printed on this page DO NOT WRITE ON THIS PAGE ANSWER IN THE SPACES PROVIDED

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